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1 <sub>P</sub>	<sup>2</sup> U	<sup>3</sup> L	⁴P	<sup>5</sup> S				6 W	<sup>7</sup> T	<sup>8</sup> S		<sup>9</sup> M	10 A	11 A
12 E	Р	Е	E	S		13 C	<sup>14</sup> R	0	Α	Т		15	N	S
16 G	R	Α	P	Н	17 T	Н	E	0	R	Υ		18 N	Α	Р
19	1	Р	S		20 H	Α	N	D	E	L		21	L	1
22 E	S	T		<sup>23</sup> M	Α	G		<sup>24</sup> S	S	Е		25 R	Υ	R
<sup>26</sup> G	E	0	27 M	E	Т	R	28 Y				29 S	Α	S	Е
			30 E	L	S	1	E		31 C	32 <b>A</b>	P	R	1	S
	33 C	34 O	М	В	1	N	Α	35 T	0	R	1	С	S	
36 C	Α	٧	E	A	Т		37 S	Н	0	R	E		* ** .	
38 A	L	E	S				39 T	0	Р	0	L	40 O	41 G	42 Y
43 V	С	R		44 A	45 M	46 S		47 R	E	W		48 P	R	E
49 E	U	R		50 L	E	T	51 T	E	R		52 G	T	0	S
53 <b>A</b>	L	A		54 P	R	0	В	Α	В	55	L	1	Т	Υ
56 R	U	T		57 H	1	N	D	U		58 D	E	N	Т	E
59 T	S	E		60 A	Т	E				61 L	E	G	0	S